Simple and Efficient Heterogeneous Graph Neural Network

Xiaocheng Yang¹, Mingyu Yan^{*1}, Shirui Pan², Xiaochun Ye¹, Dongrui Fan^{1,3}

¹ State Key Lab of Processors, Institute for Computing Technology, Chinese Academy of Sciences, China

² School of Information and Communication Technology, Griffith University, Australia

³ School of Computer Science and Technology, University of Chinese Academy of Sciences, China {yangxiaocheng, yanmingyu}@ict.ac.cn, s.pan@griffith.edu.au, {yexiaochun, fandr}@ict.ac.cn

{yangxiaocheng, yanningyu}@iet.ae.en, s.pan@grinnui.edu.au, {yexiaochun, ianui}@iet.ae.en

Abstract

Heterogeneous graph neural networks (HGNNs) have powerful capability to embed rich structural and semantic information of a heterogeneous graph into node representations. Existing HGNNs inherit many mechanisms from graph neural networks (GNNs) over homogeneous graphs, especially the attention mechanism and the multi-layer structure. These mechanisms bring excessive complexity, but seldom work studies whether they are really effective on heterogeneous graphs. This paper conducts an in-depth and detailed study of these mechanisms and proposes Simple and Efficient Heterogeneous Graph Neural Network (SeHGNN). To easily capture structural information, SeHGNN pre-computes the neighbor aggregation using a light-weight mean aggregator, which reduces complexity by removing overused neighbor attention and avoiding repeated neighbor aggregation in every training epoch. To better utilize semantic information, Se-HGNN adopts the single-layer structure with long metapaths to extend the receptive field, as well as a transformer-based semantic fusion module to fuse features from different metapaths. As a result, SeHGNN exhibits the characteristics of simple network structure, high prediction accuracy, and fast training speed. Extensive experiments on five real-world heterogeneous graphs demonstrate the superiority of SeHGNN over the state-of-the-arts on both accuracy and training speed.

Introduction

Recent years witness explosive growth in graph neural networks (GNNs) in pursuit of performance improvement of graph representation learning (Wu et al. 2020; Liu et al. 2022b; Lin et al. 2022). GNNs are primarily designed for homogeneous graphs associated with a single type of nodes and edges, following a neighborhood aggregation scheme to capture structural information of a graph, where the representation of each node is computed by recursively aggregating the features of neighbor nodes (Kipf and Welling 2017).

However, GNNs are insufficient to deal with the heterogeneous graph which possesses rich semantic information in addition to structural information (Shi et al. 2016). Many real-world data in complex systems are naturally represented as heterogeneous graphs, where multiple types of entities and relations among them are embodied by various types of nodes and edges, respectively. For example, as shown in Figure 1, the citation network ACM includes several types of nodes: Paper (P), Author (A), and Subject (S), as well as many relations with different semantic meanings, such as Author $\xrightarrow{\text{writes}}$ Paper, Paper $\xrightarrow{\text{cites}}$ Paper, Paper $\xrightarrow{\text{belongs to}}$ Subject. These relations can be composited with each other to form high-level semantic relations, which are represented as metapaths (Sun et al. 2011; Sun and Han 2012). For example, the 2-hop metapath Author-Paper-Author (APA) represents the co-author relationship and the 4-hop metapath Author-Paper-Subject-Paper-Author (APSPA) describes that the two authors have been engaged in the research of the same subject. Heterogeneous graphs contain more comprehensive information and rich semantics and require specifically designed models.

Various heterogeneous graph neural networks (HGNNs) have been proposed to capture semantic information, achieving great performance in heterogeneous graph representation learning (Dong et al. 2020; Yang et al. 2020; Wang et al. 2020; Zheng et al. 2022; Yan et al. 2022). Therefore, HGNNs are at the heart of a broad range of applications such as social network analysis (Hamilton, Ying, and Leskovec 2017a; Yasunaga et al. 2019), recommendation (Zhao et al. 2017; Hu et al. 2018), and knowledge graph inference (Chen and Sun 2017; Oh, Seo, and Lee 2018; Zhang et al. 2019b).

Figure 1 shows the two main categories of HGNNs. *Metapath-based methods* (Schlichtkrull et al. 2018; Zhang et al. 2019a; Wang et al. 2019; Fu et al. 2020) capture structural information of the same semantic first and then fuse different semantic information. These models firstly aggregate neighbor features at the scope of each metapath to generate semantic vectors, and then fuse these semantic vectors to generate the final embedding vector. *Metapath-free methods* (Zhu et al. 2019; Hong et al. 2020; Hu et al. 2020b; Lv et al. 2021) capture structural and semantic information simultaneously. These models aggregate messages from a node's local neighborhood like GNNs, but use extra modules (e.g. attentions) to embed semantic information such as node types and edge types into propagated messages.

Existing HGNNs inherit many mechanisms from GNNs over homogeneous graphs, especially the attention mechanism and the multi-layer structure, as shown in Figure 1, but

^{*}Corresponding author.

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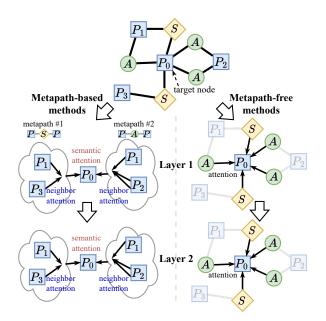


Figure 1: The general architectures of metapath-based methods and metapath-free methods on heterogeneous graphs.

seldom work studies whether these mechanisms are really effective on heterogeneous graphs. In addition, the hierarchy attention calculation in the multi-layer network and repeated neighbor aggregation in every epoch bring excessive complexity and computation. For example, the neighbor aggregation process with an attention module takes more than 85% of total time in the metapath-based model HAN (Wang et al. 2019) and the metapath-free model HGB (Lv et al. 2021), which has become the speed bottleneck for the application of HGNNs on larger-scale heterogeneous graphs.

This paper makes an in-depth and detailed study of these mechanisms and obtained two findings: (1) *semantic attention is essential while neighbor attention is not necessary*, (2) *models with single-layer structure and long metapaths perform better than those with multi-layers and short metapaths.* These findings imply that neighbor attention and multi-layer structure not only bring unnecessary complexity, but also hinder models to get better performance.

To this end, we propose a novel metapath-based method SeHGNN. SeHGNN utilizes the mean aggregator (Hamilton, Ying, and Leskovec 2017b) to simplify neighbor aggregation, adopts the single-layer structure with long metapaths to extend the receptive field, and uses a transformer-based semantic fusion module to further learn mutual attentions between semantic pairs. In addition, as the simplified neighbor aggregation is parameter-free and only contains linear operations, it earns the opportunity to execute the neighbor aggregation in the pre-processing step only once. As a result, SeHGNN not only demonstrates better performance but also avoids repeated neighbor aggregation in every training epoch, which brings a great improvement in training speed.

We conduct experiments on four widely-used datasets from HGB benchmark (Lv et al. 2021) and a large-scale dataset from OGB challenge (Hu et al. 2020a). Results show that SeHGNN achieves superior performance over the stateof-the-arts for node classification on heterogeneous graphs. The contributions of this work are summarized as follows:

- We make an in-depth study about the attention mechanism and the network structure in HGNNs and obtain two important findings, which reveal the needlessness of neighbor attention and the superiority of utilizing the single-layer structure and long metapaths.
- Motivated by the findings above, we propose a simple and effective HGNN architecture SeHGNN. To easily capture structural information, SeHGNN pre-computes the neighbor aggregation in the pre-processing step using a light-weight mean aggregator, which removes the overused neighbor attention and avoids repeated neighbor aggregation in every training epoch. To better utilize semantic information, SeHGNN adopts the singlelayer structure with long metapaths to extend the receptive field, as well as a transformer-based semantic fusion module to fuse features from different metapaths.
- Experiments on five widely-used datasets demonstrate the superiority of SeHGNN over the state-of-the-arts, i.e., high prediction accuracy and fast training speed.

Preliminaries

Definition 1 Heterogeneous graphs. A heterogeneous graph is defined as $G = \{V, E, T^v, T^e\}$, where V is the set of nodes with a node type mapping function $\phi : V \to T^v$, and E is the set of edges with an edge type mapping function $\psi : E \to T^e$. Each node $v_i \in V$ is attached with a node type $c_i = \phi(v_i) \in T^v$. Each edge $e_{t \leftarrow s} \in E$ (e_{ts} for short) is attached with a relation $r_{ct} \leftarrow c_s = \psi(e_{ts}) \in T^e$ (r_{ctcs} for short), pointing from the source node s to the target node t. When $|\mathcal{T}^v| = |\mathcal{T}^e| = 1$, the graph degenerates into homogeneous.

The graph structure of G can be represented by a series of adjacency matrices $\{A_r : r \in \mathcal{T}^e\}$. For each relation $r_{c_tc_s} \in \mathcal{T}^e$, $A_{c_tc_s} \in \mathbb{R}^{|V^{c_t}| \times |V^{c_s}|}$ is the corresponding adjacency matrix where the nonzero values indicate positions of edges $E^{c_tc_s}$ of the current relation.

Definition 2 *Metapaths.* A metapath defines a composite relation of several edge types, represented as $\mathcal{P} \triangleq c_1 \leftarrow c_2 \leftarrow \ldots \leftarrow c_l \ (\mathcal{P} = c_1c_2 \ldots c_l \text{ for short}).$

Given the metapath \mathcal{P} , a **metapath instance** p is a node sequence following the schema defined by \mathcal{P} , represented as $p(v_1, v_l) = \{v_1, e_{12}, v_2, \ldots, v_{l-1}, e_{(l-1)l}, v_l : v_i \in V^{c_i}, e_{i(i+1)} \in E^{c_i c_{i+1}}\}$. In particular, $p(v_1, v_l)$ indicates the relationship of (l-1)-hop neighborhood where v_1 is the target node and v_l is one of v_1 's **metapath-based neighbors**.

Given a metapath \mathcal{P} with the node types of its two ends as c_1, c_l , a **metapath neighbor graph** $G^{\mathcal{P}} = \{V^{c_1} \bigcup V^{c_l}, E^{\mathcal{P}}\}$ can be constructed out of G, where an edge $e_{ij} \in E^{\mathcal{P}}, \phi(i) = c_1, \phi(j) = c_l$ exists in $G^{\mathcal{P}}$ if and only if there is an metapath instance $p(v_i, v_j)$ of \mathcal{P} in G.

Related Work

For homogeneous graphs, GNNs are widely used to learn node representation from the graph structure. The pioneer GCN (Kipf and Welling 2017) proposes a multi-layer network following a layer-wise propagation rule, where the l^{th} layer learns an embedding vector $h_v^{(l+1)}$ by aggregating features { $h_u^{(l)} : u \in \mathcal{N}_v$ } from the local 1-hop neighbor set \mathcal{N}_v for each node $v \in V$. GraphSAGE (Hamilton, Ying, and Leskovec 2017b) improves the scalability for large graphs by introducing mini-batch training and neighbor sampling (Liu et al. 2022a). GAT (Veličković et al. 2018) introduces the attention mechanism to encourage the model to focus on the most important part of neighbors. SGC (Wu et al. 2019) removes nonlinearities between consecutive graph convolutional layers, which brings great acceleration and does not impact model effects.

Heterogeneous graphs contain rich semantics besides structural information, revealed by multiple types of nodes and edges. According to the way to deal with different semantics, HGNNs are categorized into metapath-based and metapath-free methods. Metapath-based HGNNs aggregate neighbor features of the same semantic first and then fuse different semantics. RGCN (Schlichtkrull et al. 2018) is the first to separate 1-hop neighbor aggregation according to different semantics. It partitions the graph into subgraphs where each subgraph contains one unique edge type. Het-GNN (Zhang et al. 2019a) takes use of neighbors of different hops. It uses random walks to collect neighbors of different distances and then aggregates neighbors of the same node type together. HAN (Wang et al. 2019) utilizes metapaths to distinguish different semantics. It firstly aggregates structural information with neighbor attention in each metapath neighbor graph in the neighbor aggregation step, and then fuses outputs from different subgraphs with semantic attention for each node in the semantic fusion step. MAGNN (Fu et al. 2020) further leverages all nodes in a metapath instance rather than only the nodes of the two endpoints.

Metapath-free HGNNs aggregate messages from neighbors in the local 1-hop neighborhood like GNNs no matter what their node types are, but using extra modules such as attentions to embed semantic information such as node types and edge types into propagated messages. RSHN (Zhu et al. 2019) firstly builds the coarsened line graph to obtain the global embedding representation of different edge types, and then it uses the combination of neighbor features and edgetype embeddings for feature aggregation in each layer. Het-SANN (Hong et al. 2020) uses a multi-layer GAT network with type-specific score functions to generate attentions for different relations. HGT (Hu et al. 2020b) proposes a novel heterogeneous mutual attention mechanism based on Transformer (Vaswani et al. 2017), using type-specific trainable parameters for different types of nodes and edges. HGB (Lv et al. 2021) takes the multi-layer GAT network as the backbone and utilizes both node features and learnable edge-type embeddings for attention generation.

Except for the above two main categories of HGNNs, SGC-based work such as NARS (Yu et al. 2020), SAGN (Sun, Gu, and Hu 2021), and GAMLP (Zhang et al. 2022) also gets impressive results on heterogeneous graphs, but they aggregate features of all types of nodes together without explicitly distinguishing different semantics.

	DB	SLP	ACM		
	macro-f1	micro-f1	macro-f1	micro-f1	
HAN	92.59	93.06	90.30	90.15	
HAN*	92.75	93.23	90.61	90.48	
HAN^{\dagger}	92.19	92.66	89.78	89.67	
HGB	94.15	94.53	93.09	93.03	
HGB*	94.20	94.58	93.11	93.05	
$\mathrm{H}\mathrm{G}\mathrm{B}^\dagger$	93.77	94.15	92.32	92.27	

Table 1: Experiments to analyze the effects of two kinds of attentions. * means removing neighbor attention and † means removing semantic attention.

	DBLP		ACM		
network	macro-f1	micro-f1	macro-f1	micro-f1	
(1,)	79.43	80.16	89.81	90.03	
(1,1)	85.06	86.69	90.79	90.87	
(2,)	88.18	88.83	91.64	91.67	
(1,1,1)	88.38	89.37	87.95	88.84	
(3,)	93.33	93.72	92.67	92.64	
(1,1,1,1)	89.55	90.44	88.62	88.93	
(2,2)	91.88	92.35	92.57	92.53	
(4)	93.60	94.02	92.82	92.79	

Table 2: Experiments to analyze the effects of different combinations of the number of layers and the maximum metapath hop. e.g., the structure (1,1,1) means a three-layer network with all metapaths no more than 1 hop in each layer.

Motivation

Existing HGNNs inherit many mechanisms from GNNs without analysis of their effects. In this section, we make an in-depth and detailed study of widely-used mechanisms, i.e. the attention mechanism and multi-layer structure for HGNNs and obtain two important findings through experiments, which help us to propose the key ideas in designing the architecture of SeHGNN. All results in this section are the average of 20 times running with different data partitions to mitigate the influence of random noise.

Study on attentions. HGNNs use multiple attentions as shown in Figure 1, which are calculated with different modules or parameters. We categorize attentions into two types, *neighbor attention* within neighbors of the same relation and *semantic attention* among different relations. Metapathbased methods like HAN use two attentions in neighbor aggregation and semantic fusion step, respectively. Metapathfree methods like HGB calculate attentions of 1-hop neighbors with relation-specific embeddings. Although it is hard to distinguish the two attentions in metapath-free methods, we can add additional calculations to eliminate the influence of either attention. Specifically, we can average attention values within each relation of each node's neighbors which equals removing neighbor attention, or normalize attention.

Re-implement experiments on HGB reveal that a welltrained HGB model tends to assign similar attention values within each relation to neighbors of each node, which pro-

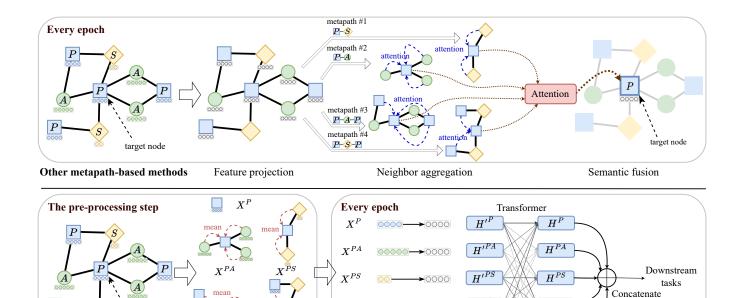


Figure 2: The architecture of SeHGNN compared to previous metapath-based methods. The example is based on ACM dataset with node types author (A), paper (P), and subject (S). This figure exhibits aggregation of 0-hop metapath P (the target node itself), 1-hop metapaths PA, PS, and 2-hop metapaths PAP, PSP.

Feature projection

 X^{PAP}

 X^{PSP}

motes us to study the necessity of different attentions. Experiments are conducted on HAN and HGB, where * means removing neighbor attention and † means removing semantic attention. Results in Table 1 show that models without semantic attention display a decrease of model effects while models without neighbor attention do not, from which we obtain the first finding.

 X^{PAP}

 X^{PSF}

target node

Neighbor aggregation

SeHGNN

Finding 1: Semantic attention is essential while neighbor attention is not necessary. This finding is reasonable as semantic attention is able to weigh the importance of different semantics, and for neighbor attention, various SGC-based work (Wu et al. 2019; Rossi et al. 2020; Zhang et al. 2022) has demonstrated that simple mean aggregation can be as effective as that with attention modules.

Study on multi-layer structure. Without neighbor attention, metapath-free methods have an equivalent form that firstly averages features of neighbors within each relation and then fuses outputs of different relations. Therefore, they can be converted to metapath-based methods with multilayer structure and only 1-hop metapaths in each layer. So, in the following experiments, we focus on the influence of number of layers and metapaths in metapath-based methods.

Experiments are conducted on HAN and we use a list of numbers to represent the structure of each variant. As examples on ACM dataset, (1,1,1,1) means a four-layer network with 1-hop metapaths PA, PS in each layer, and (4) means a single-layer network with all metapaths no more than 4-hop, e.g., PA, PS, PAP, PSP, PAPAP, PSPSP and so on. These lists also exhibit the sizes of receptive field. For example, structures (1,1,1,1), (2,2), (4) have the same size of receptive field which involves 4-hop neighbors. We conclude the second finding out of results shown in Table 2.

 H^{PAP}

 H^{PSP}

Semantic fusion

 H'^{PAP}

 H'^{PSP}

Finding 2: Models with single-layer structure and long metapaths perform better than those with multi-layers and short metapaths. Results in Table 2 show that under the same size of the receptive field, models with single-layer structure and long metapaths have better performance. We attribute this phenomenon to that multi-layer networks perform semantic fusion in each layer, making high-level semantics indistinguishable. For example, we can easily distinguish high-level semantics such as being written by the same author (PAP) or familiar authors (PAPAP) through metapaths in models with structure (4), which is unavailable for a fourlayer network (1,1,1,1) as all intermediate vectors between two consecutive layers are mixture of different semantics. In addition, increasing the maximum metapath length could enhance model effects as it brings more metapaths with different semantics.

Proposal of SeHGNN. Motivated by the two findings, on one hand, we can avoid redundant neighbor attention by using the mean aggregation at the scope of each metapath without sacrificing model effects. On the other hand, we can simplify the network structure with a single layer but use more and longer metapaths to enlarge the receptive field, which also brings better performance. In addition, as the neighbor aggregation part contains only linear operations and no trainable parameters without the attention module, it endows an opportunity to execute neighbor aggregation in the pre-processing step only once rather than in every training epoch, which significantly reduces the training time. These optimizations simplify the network structure and make it more efficient, which are the key points of SeHGNN.

Methodology

This section formally proposes Simple and Efficient Heterogeneous Neural Network (SeHGNN), a metapath-based method for heterogeneous graphs. Figure 2 shows the architecture of SeHGNN which consists of three main components: simplified neighbor aggregation, multi-layer feature projection, and transformer-based semantic fusion. Figure 2 also highlights the difference between SeHGNN and other metapath-based HGNNs, i.e., SeHGNN pre-computes the neighbor aggregation in the pre-processing step rather than in every training epoch, which reduces the excessive complexity brought from repeated neighbor aggregation. Algorithm 1 outlines the overall training process.

Simplified Neighbor Aggregation

The simplified neighbor aggregation is executed only once in the pre-processing step and generates a list of feature matrices $M = \{X^{\mathcal{P}} : \mathcal{P} \in \Phi_X\}$ of different semantics for the set Φ_X of all given metapaths. Generally, for each node v_i , it uses the mean aggregator to aggregate features from the set of metapath-based neighbors for each given metapath, and outputs a list of semantic feature vectors,

$$m_i = \{ \mathbf{z}_i^{\mathcal{P}} = \frac{1}{||S^{\mathcal{P}}||} \sum_{p(i,j) \in S_{\mathcal{P}}} \mathbf{x}_j : \mathcal{P} \in \Phi_X \},\$$

where $S^{\mathcal{P}}$ is the set of all metapath instances corresponding to metapath \mathcal{P} and p(i, j) is one metapath instance with the target node i and the source node j.

To simplify the collection of metapath-based neighbors, we propose a new method using the multiplication of adjacency matrices. Existing metapath-based methods like HAN build metapath neighbor graphs that enumerate all metapathbased neighbors for each metapath in the pre-processing step, which brings a high overhead as the number of metapath instances grows exponentially with the length of the metapath. Inspired by the layer-wise propagation of GCN, we use the multiplication of adjacency matrices to calculate the final contribution weight of each node to targets. Specifically, let $X^c = \{x_0^{c^T}; x_1^{c^T}; \dots; x_{||V^c||-1}^{c}\} \in \mathbb{R}^{||V^c|| \times d^c}$ be the raw feature matrix of all nodes belonging to type c, where d^c is the feature dimension. Then the simplified neighbor aggregation process can be expressed as

$$X^{\mathcal{P}} = \hat{A}_{c,c_1} \hat{A}_{c_1,c_2} \dots \hat{A}_{c_{l-1},c_l} X^{c_l},$$

where $\mathcal{P} = cc_1c_2 \dots c_l$ is a *l*-hop metapath, and $\hat{A}_{c_i,c_{i+1}}$ is the row-normalized form of adjacency matrix $A_{c_i,c_{i+1}}$ between node type c_i and c_{i+1} . Please note that, the aggregation results of short metapaths can be used as intermediate values for long metapaths. For example, given two metapaths PAP and PPAP for the ACM dataset, we can calculate X^{PAP} first and then calculate $X^{PPAP} = \hat{A}_{PP}X^{PAP}$. Algorithm 1: The overall training process of SeHGNN

Input: Raw feature matrices $\{X^{c_i} : c_i \in \mathcal{T}^v\}$; the raw label matrix Y; metapath sets Φ_X for features and Φ_Y for labels **Parameter**: MLP_{P_i} for feature projection; W_Q , W_K , W_V , β for semantic fusion; MLP for downstream tasks

Output: Node classification results Pred for target type c

- 1: % Neighbor aggregation
- 2: Calculate aggregation of raw features for each $\mathcal{P} \in \Phi_X$ $X^{\mathcal{P}} = A_{c,c_1} \dots A_{c_{l-1}c_l} X^{c_l}, \quad \mathcal{P} = cc_1 \dots c_{l-1}c_l$ 3: Calculate aggregation of labels for each $\mathcal{P} \in \Phi_Y$
- $Y^{\mathcal{P}} = \operatorname{rm}_{\operatorname{diag}}(A_{c,c_1} \dots A_{c_{l-1}c})Y, \quad \mathcal{P} = cc_1 \dots c_{l-1}c$ 4: Collect all semantic matrices $M = \{X^{\mathcal{P}} : \mathcal{P} \in \Phi_X\} \bigcup \{Y^{\mathcal{P}} : \mathcal{P} \in \Phi_Y\}$
- 5: for each epoch do
- % Feature projection 6:
- $H'^{\mathcal{P}_i} = \mathrm{MLP}_{\mathcal{P}_i}(M^{\mathcal{P}_i}), \ M^{\mathcal{P}_i} \in M$ 7:
- 8:
- $M = \operatorname{MLL}_{\mathcal{P}_i(M}, \mathcal{P}_i, \mathcal{M} = \mathcal{P}_i$ % Semantic fusion $Q^{\mathcal{P}_i} = W_Q H'^{\mathcal{P}_i}, K^{\mathcal{P}_i} = W_K H'^{\mathcal{P}_i}, V^{\mathcal{P}_i} = W_V H'^{\mathcal{P}_i}$ 9:

10:
$$\alpha_{ij} = \frac{\exp\left(Q^{\mathcal{P}_i \cdot K^{\mathcal{P}_j}}\right)}{\sum_{i} \exp\left(Q^{\mathcal{P}_i \cdot K^{\mathcal{P}_t}}\right)}$$

- $\begin{aligned} \alpha_{ij} &= \frac{1}{\sum_{t} \exp\left(Q^{\mathcal{P}_i \cdot K^{\mathcal{P}_t T}\right)}} \\ H^{\mathcal{P}_i} &= \beta \sum_{j} \alpha_{ij} V^{\mathcal{P}_i} + {H'}^{\mathcal{P}_i} \end{aligned}$ 11:
- $H^{c} = \text{concatenate}([H^{\mathcal{P}_{1}}||H^{\mathcal{P}_{2}}||\ldots])$ 12:
- 13: % Downstream tasks
- 14: $\operatorname{Pred} = \operatorname{MLP}(H^c)$
- 15: Calculate loss function $\mathcal{L} = -\sum_i y_i \ln pred_i$, do back-propagation and update network parameters

16: end for

17: return Pred

Besides, previous work (Wang and Leskovec 2020; Wang et al. 2021; Shi et al. 2021) proves that using labels as extra inputs provides enhancements in model effects, so we consider the aggregation of labels as well. Similar to the aggregation of raw features, the one-hot format labels can be propagated along various metapaths, generating a series of matrices $\{Y^{\mathcal{P}}: \mathcal{P} \in \Phi_Y\}$ that reflect the label distribution of corresponding metapath neighbor graphs. Please note that the two ends of any metapath $\mathcal{P} \in \Phi_Y$ should be the target node type c in the node classification task. Given a metapath $\mathcal{P} = cc_1c_2\ldots c_{l-1}c \in \Phi_Y$, the label propagation process can be represented as

$$Y^{\mathcal{P}} = \operatorname{rm_diag}(\hat{A}^{\mathcal{P}})Y^{c}, \, \hat{A}^{\mathcal{P}} = \hat{A}_{c,c_{1}}\hat{A}_{c_{1},c_{2}}\dots\hat{A}_{c_{l-1},c},$$

where Y^c is the raw label matrix. In matrix Y^c , rows corresponding to nodes in the training set take the values of onehot format labels, and other rows are filled with 0. For the aim of avoiding label leakage, we prevent each node from receiving the ground truth label information of itself, by removing the diagonal values in the results of multiplication of adjacency matrices. The label propagation also executes in the neighbor aggregation step and outputs semantic matrices as extra inputs for later training.

Multi-layer Feature Projection

The feature projection step projects semantic vectors into the same data space, as semantic vectors of different metapaths may have different dimensions or lie in different data

		DE	BLP	IM	DB	AC	CM	Free	base
		macro-f1	micro-f1	macro-f1	micro-f1	macro-f1	micro-f1	macro-f1	micro-f1
	RGCN	91.52±0.50	92.07±0.50	58.85±0.26	62.05±0.15	91.55±0.74	91.41±0.75	46.78±0.77	58.33±1.57
1st	HetGNN	91.76±0.43	92.33±0.41	48.25±0.67	51.16±0.65	85.91±0.25	86.05±0.25	-	-
151	HAN	91.67±0.49	92.05±0.62	57.74±0.96	64.63±0.58	90.89±0.43	90.79±0.43	21.31±1.68	54.77±1.40
	MAGNN	93.28±0.51	93.76±0.45	56.49±3.20	64.67±1.67	90.88±0.64	90.77±0.65	-	-
	RSHN	93.34±0.58	93.81±0.55	59.85±3.21	64.22±1.03	90.50±1.51	90.32±1.54	-	-
2nd	HetSANN	78.55±2.42	80.56±1.50	49.47±1.21	57.68±0.44	90.02±0.35	89.91±0.37	-	-
Ziiu	HGT	93.01±0.23	93.49±0.25	63.00±1.19	67.20±0.57	91.12±0.76	91.00±0.76	29.28±2.52	60.51±1.16
	HGB	94.01±0.24	94.46±0.22	63.53±1.36	67.36±0.57	93.42±0.44	93.35±0.45	47.72±1.48	66.29±0.45
3rd	SeHGNN	95.06±0.17	95.42±0.17	67.11±0.25	69.17±0.43	94.05±0.35	93.98±0.36	51.87±0.86	65.08±0.66
	Variant#1	93.61±0.51	94.08±0.48	64.48±0.45	66.58±0.42	93.06±0.18	92.98±0.18	33.23±1.39	57.60±1.17
4th	Variant#2	94.66±0.27	95.01±0.24	65.27±0.60	66.68±0.52	93.46±0.43	93.38±0.44	46.82±1.12	64.08±1.43
401	Variant#3	94.86±0.14	95.24±0.13	66.63±0.34	68.21±0.32	93.95±0.48	93.87±0.50	50.71±0.44	63.41±0.47
	Variant#4	94.52±0.05	94.93±0.06	64.99±0.54	66.65±0.50	93.88±0.63	93.80±0.64	35.48±1.36	60.03±1.13

Table 3: Experiment results on the four datasets from HGB benchmark, where "-" means that the models run out of memory.

spaces. Generally, it defines a semantic-specific transformation matrix $W^{\mathcal{P}}$ for each metapath \mathcal{P} and calculates ${H'}^{\mathcal{P}} = W^{\mathcal{P}}X^{\mathcal{P}}$. Further, for better representation power, for each metapath \mathcal{P} we use a multi-layer perception block MLP_{\mathcal{P}} with a normalization layer, a nonlinear layer, and a dropout layer between two consecutive linear layers, represented as

$${H'}^{\mathcal{P}} = \mathrm{MLP}_{\mathcal{P}}(\mathrm{X}^{\mathcal{P}})$$

Transformer-based Semantic Fusion

The semantic fusion step fuses semantic feature vectors and generates the final embedding vector for each node. Instead of a simple weighted sum format of semantic vectors, we propose a transformer (Vaswani et al. 2017)-based semantic fusion module to further explore the mutual relationship between each pair of semantics.

Specifically, with the pre-defined metapath list $\Phi = \{\mathcal{P}_1, \ldots, \mathcal{P}_K\}$ and projected semantic vectors $\{h'^{\mathcal{P}_1}, \ldots, h'^{\mathcal{P}_K}\}$ for each node, the transformer-based semantic fusion module learns the mutual attention for each pair of semantic vectors. For each semantic vector $h'^{\mathcal{P}_i}$, it maps the vector into a query vector $q^{\mathcal{P}_i}$, a key vector $k^{\mathcal{P}_i}$, and a value vector $v^{\mathcal{P}_i}$. The mutual attention weight $\alpha_{(\mathcal{P}_i, \mathcal{P}_j)}$ is the dot product result of the query vector $q^{\mathcal{P}_i}$ and the key vector $k^{\mathcal{P}_j}$ after a softmax normalization. The output vector $h^{\mathcal{P}_i}$ of current semantic \mathcal{P}_i is the weighted sum of all value vectors $v^{\mathcal{P}_j}$ plus a residual connection. The process of semantic fusion can be presented as

$$q^{\mathcal{P}_{i}} = W_{Q}h'^{\mathcal{P}_{i}}, \ k^{\mathcal{P}_{i}} = W_{K}h'^{\mathcal{P}_{i}}, \ v^{\mathcal{P}_{i}} = W_{V}h'^{\mathcal{P}_{i}}, \ \mathcal{P}_{i} \in \Phi,$$
$$\alpha_{(\mathcal{P}_{i},\mathcal{P}_{j})} = \frac{\exp\left(q^{\mathcal{P}_{i}} \cdot k^{\mathcal{P}_{j}}^{T}\right)}{\sum_{\mathcal{P}_{t} \in \Phi} \exp\left(q^{\mathcal{P}_{i}} \cdot k^{\mathcal{P}_{t}}^{T}\right)},$$
$$h^{\mathcal{P}_{i}} = \beta \sum_{\mathcal{P}_{j} \in \Phi} \alpha_{(\mathcal{P}_{i},\mathcal{P}_{j})} v^{\mathcal{P}_{j}} + h'^{\mathcal{P}_{i}},$$

where W_Q, W_K, W_V, β are trainable parameters shared for all metapaths.

The final embedding vector of each node is the concatenation of all those output vectors. For downstream tasks like the node classification, another MLP is used to generate prediction results,

$$\operatorname{Pred} = \operatorname{MLP}([h^{\mathcal{P}_1} || h^{\mathcal{P}_2} || \dots || h^{\mathcal{P}_{|\Phi|}}]).$$

Experiment

Experiments are conducted on four widely-used heterogeneous graphs including DBLP, ACM, IMDB, and Freebase from HGB benchmark (Lv et al. 2021), and a large-scale dataset ogbn-mag from OGB challenge (Hu et al. 2021). The details about all experiment settings and the network configurations are recorded in Appendix¹.

Results on HGB Benchmark

Table 3 shows the results of SeHGNN on four datasets compared with the results of baselines in HGB benchmark, including four metapath-based methods (1st block) and four metapath-free methods (2nd block). Results demonstrate the effectiveness of SeHGNN as it achieves the best performance over all these baselines but the second best for microfl accuracy on the Freebase dataset.

We perform comprehensive ablation studies to further validate the correctness of two findings in the Motivation section and the importance of other modules. The 4th block of Table 3 shows the results of four variants of SeHGNN.

Variant#1 utilizes GAT for each metapath in the neighbor aggregation step like HAN. Variant#2 uses the two-layer structure, where each layer has independent neighbor aggregation and semantic fusion steps, but the maximum hop of metapaths in each layer is half of that in SeHGNN to ensure that SeHGNN and its Variant#2 have the same size of receptive field. The performance gap between SeHGNN and these two variants proves that these two findings also hold for SeHGNN.

Variant#3 does not take labels as extra inputs. Variant#4 replaces the transformer-based semantic fusion with the weighted sum fusion like HAN. Please note that Variant#3 has already outperformed most baselines except the microf1 accuracy on the Freebase dataset. Results show that the

¹Appendix can be found at https://arxiv.org/abs/2207.02547. Codes are available at https://github.com/ICT-GIMLab/SeHGNN.

Mada ala	V ₂ 1: 1 - 4:	T
Methods	Validation accuracy	Test accuracy
RGCN	48.35±0.36	47.37±0.48
HGT	49.89±0.47	49.27±0.61
NARS	51.85±0.08	50.88±0.12
SAGN	52.25±0.30	51.17±0.32
GAMLP	53.23±0.23	51.63±0.22
HGT+emb	51.24±0.46	49.82±0.13
NARS+emb	53.72±0.09	52.40±0.16
GAMLP+emb	55.48±0.08	53.96±0.18
SAGN+emb+ms	55.91±0.17	54.40±0.15
GAMLP+emb+ms	57.02±0.41	55.90±0.27
SeHGNN	55.95±0.11	53.99±0.18
SeHGNN+emb	56.56±0.07	54.78±0.17
SeHGNN+ms	58.70±0.08	56.71±0.14
SeHGNN+emb+ms	59.17±0.09	57.19±0.12

Table 4: Experiment results on the large-scale dataset ogbnmag compared with other methods on the OGB leaderboard, where "emb" means using extra embeddings and "ms" means using multi-stage training.

utilization of label propagation and transformer-based fusion bring improvements in model effects.

Results on Ogbn-mag

The ogbn-mag dataset brings two extra challenges: (1) some types of nodes have no raw features, (2) target type nodes are split according to years, which causes training nodes and test nodes are of different data distribution. Existing methods usually tackle these challenges by (1) generating extra embeddings (abbreviated as *emb*) using unsupervised representation learning algorithms like ComplEx (Trouillon et al. 2016), (2) utilizing multi-stage learning (abbreviated as *ms*) which selects test nodes with confident predictions in last training stage, adds these nodes to the training set and retrains the model in the new stage (Li, Han, and Wu 2018; Sun, Lin, and Zhu 2020; Yang et al. 2021). For a comprehensive comparison, we compare results with or without these tricks. For methods without *emb*, we use randomly initialized feature vectors.

Table 4 shows the results on the large-scale dataset ogbnmag compared with baselines on the leaderboard of OGB. Results show that SeHGNN achieves superior performance over other methods under the same condition. Please note that SeHGNN with randomly initialized features even outperforms others with well-trained embeddings from additional representation learning algorithms, which reflects that SeHGNN learns more information from the graph structure.

Time Analysis

Firstly, we theoretically analyze the time complexity of Se-HGNN compared to HAN and HGB in a single training mini-batch with N target nodes, as Table 5 shows. We assume the one-layer structure with K metapaths for SeHGNN and HAN, and L-layer structure for HGB. The maximum hop of metapaths is also L to ensure the same size of receptive field. All methods use one-layer MLP for feature projection and the dimension of input and hidden vectors is D. The

	Feature	Neighbor	Semantic	Total
	projection	aggregation	fusion	
SeHGNN	$O(NKD^2)$			$O(NK^2D^2)$
HAN	$O(NKD^2)$	$O(NK\mathcal{E}_1D^2)$	$O(NKD^2)$	$O(NK\mathcal{E}_1D^2)$
HGB	$O(NLD^2)$	$O(N\mathcal{E})$	$(2^{2}D^{2})$	$O(N\mathcal{E}_2 D^2)$

Table 5: Theoretical complexity of SeHGNN, HAN and HGB in every training mini-batch.

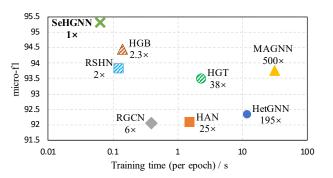


Figure 3: Micro-f1 scores and time consumption of different HGNNs on DBLP dataset. Numbers below model names exhibit the ratio of time consumption relative to SeHGNN. e.g., "6x" below RGCN means RGCN costs 6 times of time.

average number of neighbors in metapath neighbor graphs on HAN and involved neighbors during multi-layer aggregation on HGB are $\mathcal{E}_1, \mathcal{E}_2$, respectively. Please note that both \mathcal{E}_1 and \mathcal{E}_2 grow exponentially with the length of metapaths and layer number L. For the above five datasets we use tens of metapaths at most, but each node averagely aggregates information from thousands of neighbors for $L \geq 3$. Generally, we have $\mathcal{E}_1, \mathcal{E}_2 \gg K^2$, so the theoretical complexity of SeHGNN is much lower than that of HAN and HGB.

Then we conduct experiments to statistically compare the time consumption of SeHGNN with previous HGNNs. Figure 3 shows the achieving micro-f1 scores relative to the average time consumption of each training epoch for these models, which reflects that SeHGNN has advantages on both the training speed and the model effect.

Conclusion

This paper proposes SeHGNN for heterogeneous graph representation learning. Based on two findings about attention utilization and network structure, to easily capture structural information, SeHGNN pre-computes the neighbor aggregation using a light-weight mean aggregator, which avoids overused neighbor attention and repeated neighbor aggregation, and reduces the excessive complexity of HGNNs. To better utilize semantic information, SeHGNN adopts the single-layer structure with long metapaths to extend the receptive field, as well as a transformer-based semantic fusion module to fuse semantics, which greatly enhances model effects. Experiments on five widely-used datasets demonstrate the superiority of SeHGNN over the state-of-the-arts on both accuracy and training speed.

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Appendix

Observation in HGB models

The metapath-free method HGB (Lv et al. 2021) uses the concatenation of node embeddings of the two ends and the edge-type embedding to calculate the attention value for each edge, presented as

$$\alpha_{ij} = \frac{\exp(\text{LeakyReLU}(\mathbf{a}^T[\mathbf{W}\mathbf{h}_i||\mathbf{W}\mathbf{h}_j||\mathbf{W}_r\mathbf{r}_{ij}]))}{\sum_{k \in \mathcal{N}_i} \exp(\text{LeakyReLU}(\mathbf{a}^T[\mathbf{W}\mathbf{h}_i||\mathbf{W}\mathbf{h}_k||\mathbf{W}_r\mathbf{r}_{ik}]))}$$

In the re-implement experiments of HGB, we find that the attention values are mostly controlled by the edge-type embeddings, revealed by the observation that attention values within each relation are similar, while those among different

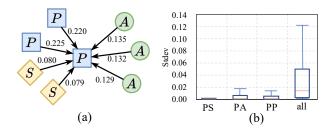


Figure 4: (a) An illustration of the observation that HGB tends to assign similar attention values within each relation for each target node. (b) The box plot of standard deviations of attention values for different relations in HGB.

	RGCN	HetGNN	HAN	MAGNN		
Feature projection	$\mathbf{h}_v' = W^{\phi(v)} \mathbf{x}_v$					
Neighbor aggregation	$\mathbf{z}_v^r = rac{1}{ \mathcal{N}_v^r } \sum_{u \in \mathcal{N}_v^r} \mathbf{h}_u'$	$\mathbf{z}_v^t = ext{Bi-LSTM}(\{\mathbf{h}_u': u \in \mathcal{N}_v^t\})$	$\alpha_{v,u}^{\mathcal{P}} = \frac{\exp(\gamma_{v,u}^{\mathcal{P}})}{\sum_{k \in \mathcal{N}_v^{\mathcal{P}}} \exp(\gamma_{v,k}^{\mathcal{P}})},$	$ \begin{split} \mathbf{h}_{p(v,u)}' &= \text{Encoder}(p(v,u)) \\ \gamma_{v,u}^{\mathcal{P}} &= \sigma(\mathbf{a}_{\mathcal{P}}^{T} \cdot [\mathbf{h}_{v}' \mathbf{h}_{p(v,u)}]) \\ \mathbf{z}_{v}^{\mathcal{P}} &= \sigma(\sum_{k \in \mathcal{N}_{v}^{\mathcal{P}}} \alpha_{v,k}^{\mathcal{P}} \mathbf{h}_{p(v,k)}') \end{split} $		
Semantic fusion	$\mathbf{h}_v = \sum_r \mathbf{z}_v^r + W_0 \mathbf{x}_v$	$ \boldsymbol{\alpha}_{v}^{t} = \frac{\exp\left(\mathrm{LeakyReLU}(\mathbf{a}^{T}[\mathbf{z}_{v}^{t} \mathbf{h}_{v}^{t}])\right)}{\sum_{k}\exp\left(\mathrm{LeakyReLU}(\mathbf{a}^{T}[\mathbf{z}_{v}^{t} \mathbf{h}_{v}^{t}])\right)} \\ \mathbf{h}_{v} = \boldsymbol{\alpha}_{v}\mathbf{h}_{v}^{t} + \sum_{t}\boldsymbol{\alpha}_{v}^{t}\mathbf{z}_{v}^{t} $	$w_{\mathcal{P}} = \frac{1}{ V^{\phi(v)} } \sum_{k \in \mathbb{N}} \delta_{\mathcal{P}_i} = \frac{\exp(w_{\mathcal{P}_i})}{\sum_{\mathcal{P}_j} \exp(w)}$	$V^{\phi(v)} \mathbf{q}^T \cdot \tanh(\mathbf{W} \mathbf{z}_k^{\mathcal{P}} + \mathbf{b})$ $\frac{\partial}{\partial P_j}, \ \mathbf{h}_v = \sum_{\mathcal{P}_i} \beta_{\mathcal{P}_i} \mathbf{z}_v^{\mathcal{P}_i}$		

Table 6: The unified framework of existing metapath-based HGNNs.

relations differ a lot. Figure 4 (a) gives a diagram of this observation and Figure 4 (b) shows the statistics of standard deviations of attention values within each relation and among all relations for each target node on the ACM dataset.

This observation promotes us to study the necessity of neighbor attention within each relation and semantic attention among different relations in HGNNs.

Framework of existing metapath-based methods

The calculation in each layer of existing metapath-based methods can be divided into three main steps, *feature projection, neighbor aggregation*, and *semantic fusion*, as shown in Table 6. The feature projection step aims to map raw feature vectors of different types of nodes into the same data space, usually presented as one linear projection layer. Then the neighbor aggregation step aggregates feature vectors of neighbors at the scope of each semantic, e.g., for each relation (can be viewed as 1-hop metapath) in RGCN, for each node type in HetGNN, or for each metapath in HAN and MAGNN. At last, the semantic aggregation step fuses those semantic vectors across all semantics and outputs the final embedding for each node.

After removing neighbor attention, as both the one-layer feature projection and neighbor aggregation contain no nonlinear functions, the order of the two steps can be exchanged. Further, as the neighbor aggregation step involves no trainable parameters, it can be put ahead in the pre-processing step and its results are shared across all training epochs.

In later experiments, we find a multi-layer block for feature projection can further enhance the performance. Therefore, SeHGNN adopts an MLP block for each metapath in the feature projection step.

Experiment settings

The evaluation of SeHGNN involves four medium-scale datasets from HGB benchmark (Lv et al. 2021) and a large-scale dataset ogbn-mag² from OGB challenge (Hu et al. 2021). Statistics of these heterogeneous graphs are summa-rized in Table 7. For the medium-scale datasets, the dataset configuration follows the requirements of HGB benchmark, where target type nodes are split with 30% for local training and 70% for online test. Labels of test nodes are not made public and researchers have to submit their predictions to the website of HGB benchmark for online evaluation. For

Dataset	#Nodes	#Node types	#Edges	#Classes
DBLP	26,128	4	239,566	4
ACM	10,942	4	547,872	3
IMDB	21,420	4	86,642	5
Freebase	180,098	8	1,057,688	7
Ogbn-mag	1,939,743	4	21,111,007	349

Table 7: Statistics of datasets used in this paper.

	Feature p	propagation	Label Propagation		
	Max Hop	#Metapaths	Max Hop	#Metapaths	
DBLP	2	5	4	4	
IMDB	4	25	4	12	
ACM	4	41	4	9	
Freebase	2	73	4	9	
Ogbn-mag	2	10	2	5	

Table 8: The maximum hops of metapaths for raw feature propagation and label propagation.

local training, we randomly split the 30% nodes with 24% for training for 6% for validation. Results are compared with scores of baselines reported in the paper of HGB and all scores are the average from 5 different local data partitions. For the ogbn-mag dataset, we follows the official data partition where papers published before 2018, in 2018, and since 2019 are nodes for training, validation, and test, respectively. Results are compared with scores on OGB leaderboard and all scores are the average from 10 separate training.

We adopt a simple metapath selection method that we preset the maximum hop and use all available metapaths no more than this maximum hop. We test different combinations of maximum hops for raw feature propagation and label propagation and the final choices are listed in Figure 8.

For all experiments, SeHGNN adopts a two-layer MLP for each metapath in the feature projection step and the dimension of hidden vectors is 512. In the transformer-based fusion module, the dimension of query and key vectors are 1/4 of hidden vectors, the dimension of value vectors equals that of hidden vectors, and the number of heads is 1.

SeHGNN is optimized with Adam (Kingma and Ba 2015) during training. The learning rate is 0.0003 and the weight decay is 0.0001 for the Freebase dataset, and the learning rate is 0.001 and the weight decay is 0 for others.

²https://ogb.stanford.edu/docs/nodeprop/#ogbn-mag